

# Grafica tridimensionale

## Oggetti grafici

**Graphics3D[primitives, options]** represents a three-dimensional graphical image. Default options: AmbientLight -> GrayLevel[0.], AspectRatio -> Automatic, Axes -> False, AxesEdge -> Automatic, AxesLabel -> None, AxesStyle -> Automatic, Background -> Automatic, Boxed -> True, BoxRatios -> Automatic, BoxStyle -> Automatic, ColorOutput -> Automatic, DefaultColor -> Automatic, Epilog -> {}, FaceGrids -> None, Lighting -> True, LightSources -> {{{{1., 0., 1.}, RGBColor[1, 0, 0]}}, {{1., 1., 1.}, RGBColor[0, 1, 0]}}, {{0., 1., 1.}, RGBColor[0, 0, 1]}}}, PlotLabel -> None, PlotRange -> Automatic, PlotRegion -> Automatic, Plot3Matrix -> Automatic, PolygonIntersections -> True, Prolog -> {}, RenderAll -> True, Shading -> True, SphericalRegion -> False, Ticks -> Automatic, ViewCenter -> Automatic, ViewPoint -> {1.3, -2.4, 2.}, ViewVertical -> {0., 0., 1.}, DefaultFont -> \$DefaultFont, DisplayFunction -> \$DisplayFunction.

**SurfaceGraphics[array]** is a representation of a three-dimensional plot of a surface, with heights of each point on a grid specified by values in array. **SurfaceGraphics[array, shades]** represents a surface, whose parts are shaded according to the array shades.

## Primitive grafiche

**Cuboid[{xmin, ymin, zmin}]** is a three-dimensional graphics primitive that represents a unit cuboid, oriented parallel to the axes. **Cuboid[{xmin, ymin, zmin}, {xmax, ymax, zmax}]** specifies a cuboid by giving the coordinates of opposite corners.

**Line[{pt1, pt2, ...}]** is a graphics primitive which represents a line joining a sequence of points.

**Point[coords]** is a graphics primitive that represents a point.

**Polygon[{pt1, pt2, ...}]** is a graphics primitive that represents a filled polygon.

**Text[expr, coords]** is a graphics primitive that represents text corresponding to the printed form of expr, centered at the point specified by coords.

**Scaled[{x, y, z}]** gives the position of a graphical object in terms of coordinates scaled to run from 0 to 1 across the whole plot in each direction.

**Scaled[{dx, dy, dz}, {x0, y0, z0}]** gives a position obtained by starting at absolute coordinates {x0, y0, z0}, then moving by a scaled offset {dx, dy, dz}.

## Direttive grafiche

**AbsoluteDashing[{d1, d2, ...}]** is a two-dimensional graphics directive which specifies that lines which follow are to be drawn dashed, with successive segments having absolute lengths d1, d2, ... (repeated cyclically). The lengths di are given in points.

**AbsolutePointSize[d]** is a graphics directive which specifies that points which follow are to be shown if possible as circular regions with absolute radius d. The radius d is given in points.

**AbsoluteThickness[d]** is a graphics directive which specifies that lines which follow are to be drawn with absolute thickness d. The thickness d is given in points.

**CMYKColor[cyan, magenta, yellow, black]** is a graphics directive which specifies that graphical objects which follow are to be displayed in the color given.

**Dashing[{r1, r2, ...}]** is a two-dimensional graphics directive which specifies that lines which follow are to be drawn dashed, with successive segments of lengths r1, r2, ... (repeated cyclically). The ri are given as a fraction of the total width of the graph.

**EdgeForm[g]** is a three-dimensional graphics directive which specifies that edges of polygons are to be drawn using the graphics directive or list of graphics directives g.

**FaceForm[*gf*, *gb*]** is a three-dimensional graphics directive which specifies that the front faces of polygons are to be drawn with the graphics primitive *gf*, and the back faces with *gb*.

**GrayLevel[*level*]** is a graphics directive which specifies the gray-level intensity with which graphical objects that follow should be displayed.

**Hue[*h*]** is a graphics directive which specifies that graphical objects which follow are to be displayed, if possible, in a color corresponding to hue *h*.

Hue[*h*, *s*, *b*] specifies colors in terms of hue, saturation and brightness.

**RGBColor[*red*, *green*, *blue*]** is a graphics directive which specifies that graphical objects which follow are to be displayed, if possible, in the color given.

**PointSize[*r*]** is a graphics directive which specifies that points which follow are to be shown if possible as circular regions with radius *r*. The radius *r* is given as a fraction of the total width of the graph.

**SurfaceColor[*dcol*]** is a three-dimensional graphics directive which specifies that the polygons which follow should act as diffuse reflectors of light with a color given by *dcol*.

SurfaceColor[*dcol*, *scol*] specifies that a specular reflection component should be included, with a color given by *scol*.

SurfaceColor[*dcol*, *scol*, *n*] specifies that the reflection should occur with specular exponent *n*.

**Thickness[*r*]** is a graphics directive which specifies that lines which follow are to be drawn with a thickness *r*. The thickness *r* is given as a fraction of the total width of the graph.

## Generazione di oggetti grafici

**Plot3D[*f*, {*x*, *xmin*, *xmax*}, {*y*, *ymin*, *ymax*}]** generates a three-dimensional plot of *f* as a function of *x* and *y*.

Plot3D[{*f*, *s*}, {*x*, *xmin*, *xmax*}, {*y*, *ymin*, *ymax*}] generates a three-dimensional plot in which the height of the surface is specified by *f*, and the shading is specified by *s*.

Default options: AmbientLight -> GrayLevel[0], AspectRatio -> Automatic, Axes -> True, AxesEdge -> Automatic, AxesLabel -> None, AxesStyle -> Automatic, Background -> Automatic, Boxed -> True, BoxRatios -> {1, 1, 0.4}, BoxStyle -> Automatic, ClipFill -> Automatic, ColorFunction -> Automatic, ColorOutput -> Automatic, Compiled -> True, DefaultColor -> Automatic, Epilog -> {}, FaceGrids -> None, HiddenSurface -> True, Lighting -> True, LightSources -> {{{1., 0., 1.}, RGBColor[1, 0, 0]}, {{1., 1., 1.}, RGBColor[0, 1, 0]}, {{0., 1., 1.}, RGBColor[0, 0, 1]}}, Mesh -> True, MeshStyle -> Automatic, PlotLabel -> None, PlotPoints -> 15, PlotRange -> Automatic, PlotRegion -> Automatic, Plot3Matrix -> Automatic, Prolog -> {}, Shading -> True, SphericalRegion -> False, Ticks -> Automatic, ViewCenter -> Automatic, ViewPoint -> {1.3, -2.4, 2.}, ViewVertical -> {0., 0., 1.}, DefaultFont :> \$DefaultFont, DisplayFunction :> \$DisplayFunction.

**ParametricPlot3D[{*fx*, *fy*, *fz*}, {*t*, *tmin*, *tmax*}]** produces a three-dimensional space curve parameterized by a variable *t* which runs from *tmin* to *tmax*.

ParametricPlot3D[{*fx*, *fy*, *fz*}, {*t*, *tmin*, *tmax*}, {*u*, *umin*, *umax*}] produces a three-dimensional surface parameterized by *t* and *u*.

ParametricPlot3D[{*fx*, *fy*, *fz*, *s*}, ...] shades the plot according to the color specification *s*.

ParametricPlot3D[{{*fx*, *fy*, *fz*}, {*gx*, *gy*, *gz*}, ...}, ...] plots several objects together.

Default options: AmbientLight -> GrayLevel[0.], AspectRatio -> Automatic, Axes -> True, AxesEdge -> Automatic, AxesLabel -> None, AxesStyle -> Automatic, Background -> Automatic, Boxed -> True, BoxRatios -> Automatic, BoxStyle -> Automatic, ColorOutput -> Automatic, Compiled -> True, DefaultColor -> Automatic, Epilog -> {}, FaceGrids -> None, Lighting -> True, LightSources -> {{{1., 0., 1.}, RGBColor[1, 0, 0]}, {{1., 1., 1.}, RGBColor[0, 1, 0]}, {{0., 1., 1.}, RGBColor[0, 0, 1]}}, PlotLabel -> None, PlotPoints -> Automatic, PlotRange -> Automatic, PlotRegion -> Automatic, Plot3Matrix -> Automatic, PolygonIntersections -> True, Prolog -> {}, RenderAll -> True, Shading -> True, SphericalRegion -> False, Ticks -> Automatic, ViewCenter -> Automatic, ViewPoint -> {1.3, -2.4, 2.}, ViewVertical -> {0., 0., 1.}, DefaultFont :> \$DefaultFont, DisplayFunction :> \$DisplayFunction.

**ListPlot3D[*array*]** generates a three-dimensional plot of a surface representing an array of height values.

ListPlot3D[array, shades] generates a plot with each element of the surface shaded according to the specification in shades.

## Visualizzazione di oggetti grafici

Show[graphics, options] displays two- and three-dimensional graphics, using the options specified.

Show[g1, g2, ...] shows several plots combined.

## Opzioni

**AmbientLight** is an option to Graphics3D and related functions that gives the level of simulated ambient illumination in a three-dimensional picture. The setting must be a GrayLevel, Hue, or RGBColor directive.

**AspectRatio** is an option for Show and related functions. With AspectRatio -> Automatic, the ratio of height to width of the plot is determined from the actual coordinate values in the plot. AspectRatio -> r makes the ratio equal to r.

**Axes** is an option for graphics functions. With Axes -> True, all axes are drawn. Axes -> False draws no axes. Axes -> {False, False, True} draws a z axis but no x or y axis.

**AxesEdge** is an option for 3D graphics functions. AxesEdge -> {{xdir, ydir}, {xdir, zdir}, {xdir, ydir}} specifies on which three edges of the bounding box axes are drawn. The idir must be either +1 or -1, and specify whether axes are drawn on the edge of the box with a larger or smaller value of coordinate i, respectively. Any pair {idir, jdir} can be replaced by Automatic or None. The default setting is AxesEdge -> Automatic.

**AxesLabel** is an option for graphics functions. With AxesLabel -> None, no labels are drawn on the axes in the plot. AxesLabel -> label specifies a label for the z axis. AxesLabel -> {xlabel, ylabel, zlabel} specifies labels for different axes.

**AxesOrigin** is an option for two-dimensional graphics functions. AxesOrigin -> {x, y} specifies that the axes drawn should cross at the point {x, y}. AxesOrigin -> Automatic uses an internal algorithm to determine where the axes should cross.

**AxesStyle** is an option for graphics functions. AxesStyle -> style specifies that all axes are to be rendered with the specified graphics directive, or list of graphics directives. AxesStyle -> {{xstyle}, {ystyle}, {zstyle}} specifies that axes should use graphics directives xstyle, zstyle.

**Background** is an option for graphics functions which specifies the background color to use. A setting must be a CMYKColor, GrayLevel, Hue or RGBColor directive. The default setting Background -> Automatic produces a white background on most output devices.

**Boxed** is an option for Graphics3D. Boxed -> True draws the edges of the bounding box in a three-dimensional picture. With Boxed -> False, no bounding box is drawn.

**BoxRatios** is an option for Graphics3D and SurfaceGraphics. BoxRatios -> {rx, ry, rz} gives the ratios of side lengths for the bounding box of the three-dimensional picture. BoxRatios -> Automatic determines the ratios using the range of actual coordinate values in the plot.

**BoxStyle** is an option for three-dimensional graphics functions which specifies how the bounding box should be rendered. BoxStyle can be set to a list of graphics directives such as Dashing, Thickness, GrayLevel and RGBColor. BoxStyle -> Automatic uses a default style.

**ColorOutput** is an option for graphics functions which specifies the type of color output to produce. ColorOutput -> Automatic uses whatever color directives are given. ColorOutput -> CMYKColor converts to CMYKColor. ColorOutput -> GrayLevel converts to GrayLevel. ColorOutput -> RGBColor converts to RGBColor. ColorOutput -> f converts using the function f.

**DefaultColor** is an option for graphics functions which specifies the default color to use for lines, points, etc. The setting must be a CMYKColor, GrayLevel, Hue or RGBColor directive. The default setting DefaultColor -> Automatic gives a color complementary to the background specified.

**DefaultFont** is an option for graphics functions which specifies the default font to use for text. DefaultFont -> {"font", size} specifies the name and size of the font to use. The default setting is DefaultFont := \$DefaultFont.

**DisplayFunction** is an option for graphics functions that specifies the function to apply to graphics primitives in order to display them. The default setting is `$DisplayFunction`. A typical setting is `DisplayFunction -> (Display[channel, #]&)`. `DisplayFunction -> Identity` causes the objects to be returned, but no display to be generated.

**Epilog** is an option for graphics functions which gives a list of graphics primitives to be rendered after the main part of the graphics is rendered.

**FaceGrids** is an option for three-dimensional graphics functions. With `FaceGrids -> All`, grid lines are drawn on all the faces of the bounding box. `FaceGrids -> None` draws no grid lines. `FaceGrids -> {face1, face2, ...}` draws grid lines on the specified faces. `FaceGrids -> {{face1, {xgrid, ygrid}}, ...}` specifies an arrangement of the grid lines.

**Lighting** is an option to `Graphics3D` and related functions. With `Lighting -> True`, simulated illumination is used; with `Lighting -> False`, it is not.

**LightSources** is an option to `Graphics3D` and related functions that specifies the properties of point light sources for simulated illumination. The basic form is `LightSources -> {{direction1, color1}, {direction2, color2}, ...}`. The direction is specified as `{x, y, z}`. The color can be specified by `GrayLevel`, `Hue` or `RGBColor`.

**PlotLabel** is an option for graphics functions that specifies an overall label for a plot. With `PlotLabel -> None`, no label is given. `PlotLabel -> label` specifies a label.

**PlotRange** is an option for graphics functions. With `PlotRange -> All`, all points are included in the plot. With `PlotRange -> Automatic`, outlying points are dropped. `PlotRange -> {min, max}` specifies explicit limits for `z`. `PlotRange -> {{xmin, xmax}, {ymin, ymax}, {zmin, zmax}}` gives explicit limits for each coordinate.

**PlotRegion** is an option for graphics functions. `PlotRegion -> {{sxmin, sxmax}, {symin, symax}}` specifies the region in scaled coordinates that the plot should fill in the final display area. With `PlotRegion -> Automatic`, the plot fills the final display area.

**PolygonIntersections** is an option for `Graphics3D` and `ParametricPlot3D`. With `PolygonIntersections -> True`, intersecting polygons are left unchanged. With `PolygonIntersections -> False`, `Graphics3D` objects are modified by breaking polygons into smaller pieces which do not intersect each other.

**Prolog** is an option for graphics functions which gives a list of graphics primitives to be rendered before the main part of the graphics is rendered.

**RenderAll** is an option to `Graphics3D`. When `RenderAll -> False`, `PostScript` will be generated only for those polygons or parts of polygons which are visible in the final picture. If `RenderAll -> True`, `PostScript` is generated for all polygons.

**RotateLabel** is an option for two-dimensional graphics functions. With `RotateLabel -> True`, labels on vertical frame axes are rotated to be vertical. With `RotateLabel -> False`, they are not.

**Shading** is an option for `SurfaceGraphics`. With `Shading -> True`, surfaces are shaded. With `Shading -> False`, they are not.

**SphericalRegion** is an option for three-dimensional graphics functions. With `SphericalRegion -> True`, the final image is scaled so that a sphere drawn around the three-dimensional bounding box will fit in the display area specified. `SphericalRegion -> False` scales three-dimensional images to be as large as possible, given the display area specified.

**Ticks** is an option for graphics functions. With `Ticks -> None`, no tick marks are drawn on the axes. With `Ticks -> Automatic`, tick marks are placed automatically. `Ticks -> {xticks, yticks, zticks}` specifies tick mark options separately for each axis.

**ViewCenter** is an option for `Graphics3D` and `SurfaceGraphics`. With `ViewCenter -> Automatic`, the whole bounding box is centered in the final image area. With `ViewCenter -> {x, y, z}`, the point in the three-dimensional bounding box with scaled coordinates `x, y, z` is placed at the center of the final display area.

**ViewPoint** is an option for Graphics3D and SurfaceGraphics which gives the point in space from which the objects plotted are to be viewed. ViewPoint  $\rightarrow$   $\{x, y, z\}$  gives the position of the view point relative to the center of the three-dimensional box that contains the object being plotted.

**ViewVertical** is an option for Graphics3D and SurfaceGraphics. ViewVertical  $\rightarrow$   $\{x, y, z\}$  specifies the direction in scaled coordinates which should be vertical in the final image.