

## Calcolo numerico

**Integer** is the head used for integers.

**Rational** is the head used for rational numbers.

**Real** is the head used for real (floating-point) numbers.

**Complex** is the head used for complex numbers.

### Numeri interi

**IntegerQ[expr]** gives True if expr is an integer, and False otherwise.

**EvenQ[expr]** gives True if expr is an even integer, and False otherwise.

**OddQ[expr]** gives True if expr is an odd integer, and False otherwise.

**PrimeQ[expr]** yields True if expr is a prime number, and yields False otherwise.

In the current version of Mathematica, the algorithm used for large integers is probabilistic, but very reliable (pseudoprime test and Lucas test).

**IntegerDigits[n]** gives a list of the decimal digits in the integer n.

**IntegerDigits[n, b]** gives a list of the base-b digits in the integer n.

**IntegerDigits[n, b, k]** gives a list of length k containing the least significant digits of n.

**Quotient[n, m]** gives the integer quotient of n and m, defined as  $\text{Floor}[n/m]$ .

**Mod[m, n]** gives the remainder on division of m by n. The result has the same sign as n.

**GCD[n1, n2, ...]** gives the greatest common divisor of the integers ni.

**LCM[n1, n2, ...]** gives the least common multiple of the integers ni.

**FactorInteger[n]** gives a list of the prime factors of the integer n, together with their exponents.

**Divisors[n]** gives a list of the integers that divide n.

**EulerPhi[n]** gives the Euler totient function  $\phi(n)$ . It is the number of positive integers less than n which are relatively prime to n.

**Prime[n]** gives the nth prime number.

**PrimePi[n]** gives the number of primes less than or equal to n.

**n!** gives the factorial of n.

**Binomial[n, m]** gives the binomial coefficient.

**Multinomial[n1, n2, ...]** gives the multinomial coefficient  $(n1+n2+\dots)!/(n1! n2! \dots)$ .

### Numeri "reali"

**NumberQ[expr]** gives True if expr is a number, and False otherwise.

**N[expr]** gives the numerical value of expr.

**N[expr, n]** does computations to n-digit precision.

**Positive[x]** gives True if x is a positive number.

**Negative[x]** gives True if x is a negative number.

**Sign[x]** gives -1, 0 or 1 depending on whether x is negative, zero, or positive.

**Sign[z]** gives the sign of the complex number z.

**RealDigits[x]** gives a list of the digits in the approximate real number x, together with the number of digits that appear to the left of the decimal point in scientific notation.

**RealDigits[x, b]** gives a list of base-b digits in x.

**Floor[x]** gives the greatest integer less than or equal to x.

**Ceiling[x]** gives the smallest integer greater than or equal to x.

**Round[x]** gives the integer closest to x.

**Rationalize[x]** takes Real numbers in x that are close to rationals, and converts them to exact Rational numbers.  
**Rationalize[x, dx]** performs the conversion whenever the error made is smaller in magnitude than dx.

**Chop[expr]** replaces approximate real numbers in expr that are close to zero by the exact integer 0.  
**Chop[expr, tol]** replaces approximate real numbers in expr that differ from zero by less than tol with 0.

**Random[ ]** gives a uniformly distributed pseudorandom Real in the range 0 to 1.  
**Random[type, range]** gives a pseudorandom number of the specified type, lying in the specified range. Possible types are: Integer, Real and Complex. The default range is 0 to 1. You can give the range {min, max} explicitly; a range specification of max is equivalent to {0, max}.

**SeedRandom[n]** resets the pseudorandom number generator, using the integer n as a seed.  
**SeedRandom[ ]** resets the generator, using as a seed the time of day.

## Intervalli

**Interval[{min, max}]** represents the range of values between min and max.  
**Interval[{a,b}, {c,d}, ...]** represents the union of the ranges a to b, c to d, ....

**IntervalMemberQ[int, x]** gives True if the number x is in the interval int, False otherwise.  
**IntervalMemberQ[int1, int2]** gives True if the interval int2 is contained within the interval int1.

**IntervalUnion[int1, int2, ...]** gives an interval representing the union of the intervals int1, int2, ....

**IntervalIntersection[int1, int2, ...]** gives an interval representing the intersection of the intervals int1, int2, ....

## Fuzioni numeriche

**NSum[f, {i, imin, imax}]** gives a numerical approximation to the sum of f with i running from imin to imax.  
**NSum[f, {i, imin, imax, di}]** uses a step di in the sum.  
**NSum[f, {i, imin, imax}, {j, jmin, jmax}, ...]** gives a multi-dimensional summation.

**NProduct[f, {i, imin, imax}]** gives a numerical approximation to the product of f with i running from imin to imax.  
**NProduct[f, {i, imin, imax, di}]** uses a step di in the product.

**FindMinimum[f, {x, x0}]** searches for a local minimum in f, starting from the point x=x0.

**ConstrainedMax[f, {inequalities}, {x, y, ...}]** finds the global maximum of f in the domain specified by the inequalities. The variables x, y, ... are all assumed to be non-negative.

**ConstrainedMin[f, {inequalities}, {x, y, ...}]** finds the global minimum of f in the domain specified by the inequalities. The variables x, y, ... are all assumed to be non-negative.

**FindRoot[lhs == rhs, {x, x0}]** searches for a numerical solution to the equation lhs == rhs, starting with x == x0.

**NSolve[eqns, vars]** attempts to solve numerically an equation or set of equations for the variables vars. Any variable in eqns but not vars is regarded as a parameter.  
**NSolve[eqns]** treats all variables encountered as vars above.  
**NSolve[eqns, vars, prec]** attempts to solve numerically the equations for vars using prec digits precision.

**NDSolve**[eqns, y, {x, xmin, xmax}] finds a numerical solution to the differential equations eqns for the function y with the independent variable x in the range xmin to xmax.

**NDSolve**[eqns, {y1, y2, ...}, {x, xmin, xmax}] finds numerical solutions for the functions yi.

**NDSolve**[eqns, y, {x, x1, x2, ...}] forces a function evaluation at each of x1, x2, ... The range of numerical integration is from Min[x1, x2, ...] to Max[x1, x2, ...].

**NIntegrate**[f, {x, xmin, xmax}] gives a numerical approximation to the integral of f with respect to x over the interval xmin to xmax.

**Interpolation**[data] constructs an InterpolatingFunction object which represents an approximate function that interpolates the data. The data can have the forms {{x1, f1}, {x2, f2}, ...} or {f1, f2, ...}, where in the second case, the xi are taken to have values 1, 2, ....

**Fit**[data, funs, vars] finds a least-squares fit to a list of data as a linear combination of the functions funs of variables vars. The data can have the form {{x1, y1, ..., f1}, {x2, y2, ..., f2}, ...}, where the number of coordinates x, y, ... is equal to the number of variables in the list vars. The data can also be of the form {f1, f2, ...}, with a single coordinate assumed to take values 1, 2, .... The argument funs can be any list of functions that depend only on the objects vars.